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ADDENDUM TO “RINGS WHOSE MODULES HAVE MAXIMAL SUBMODULES”

CARL FAITH

A ring R is *right max* if every nonzero right R -module has a maximal submodule. In [F1] the author stated several open problems regarding right max rings.

Let E be the minimal injective cogenerator of $\text{mod-}R$, and let $\Lambda = \text{End}(E_R)$ be its endomorphism ring.

- (1) If Λ is right max, is R ?
- (2) If R is right max, is Λ ?

Recently, Xue [X] answered (1) in the affirmative, and (2) in the negative. He also appended several typos in [F1], which we list here for the convenience of the readers of *Publicacions Matemàtiques*.

Corrections to [F1]

- (C1) p. 202, l. 6: replace “iff” by “only if”. For a perfect local ring R the unique simple module E has the stated property but does not cogenerate $\text{mod-}R$ unless R is a field.
- (C2) p. 203, footnote: “semi-Artinian” should be “Artinian”. (A 2-sided perfect ring R is semi-Artinian and Hamsher but need not be Noetherian.)
- (C3) p. 212, l. 10–11: “right and left Artinian” should be “right Artinian” for a right Morita duality, and left Artinian for a left Morita duality, since a right Artinian ring with a right Morita duality need not be left Artinian. (See [T, p. 32, Theorem 3.7 and p. 37].)
- (C4) p. 214, l. 11: “4 (1966), 373–387” ought to be “16 (1970), 60–66”.
- (C5) p. 203, **First and Second Max Theorem**: add Renault [R] to the cited references [H], [K].

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Remarks. (1) As Xue [X] remarks, these corrections in no way affect the results of [F1].

(2) The Abstract [F3] listed in [F1] has since appeared as [F2] below.

References

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Rutgers University
Department of Mathematics
New Brunswick, NJ 08903
U.S.A.

Author Permanent Address:
199 Longview Drive
Princeton, NJ 08540
U.S.A.

e-mail: carlfaith@aol.com

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